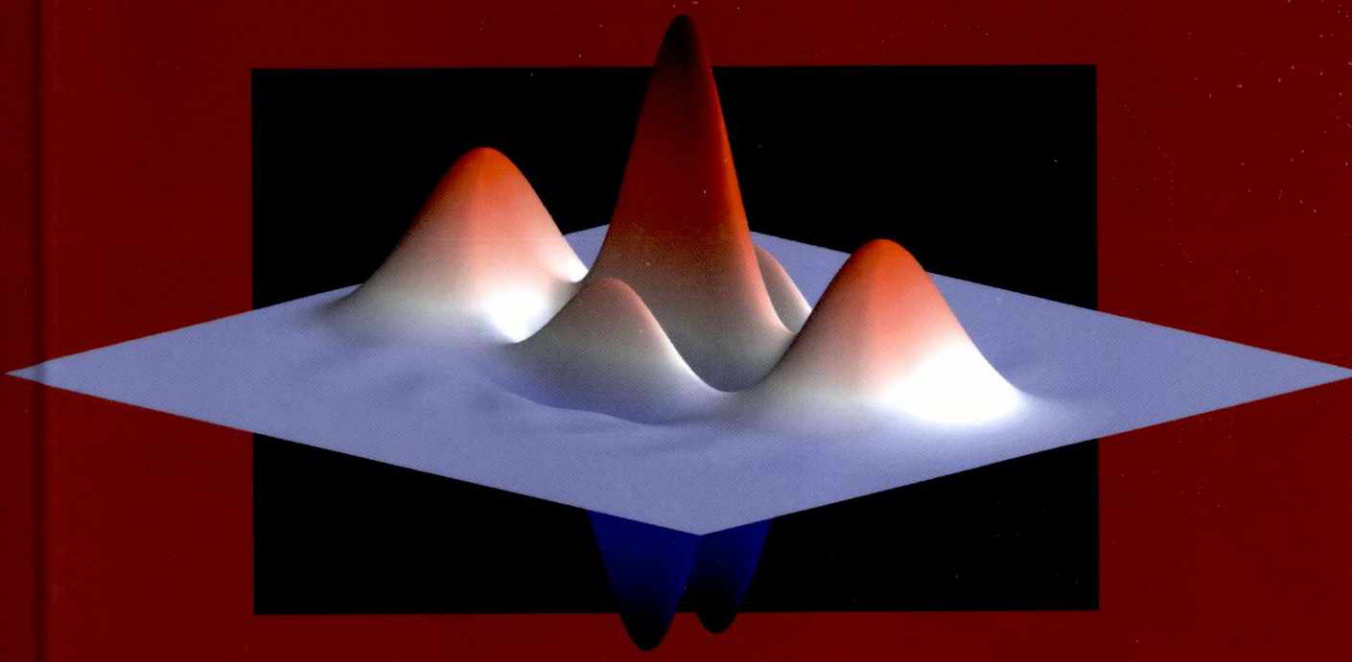
INTRODUCTORY QUANTUM OPTICS

SECOND EDITION



Christopher C. Gerry
Peter L. Knight

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